

**Simulation Based on Michel Fodje's epr-simple simulation translated from Python to Mathematica by John Reed 13 Nov 2013**  
**Modified by Fred Diether for Completely Local-Realistic July 2021**  
**Some parts by Bill Nelson. Includes Joy's  $S^3$  Quaternion Model.**

Set Run Time Parameters, Initialize Arrays and Tables

```
In[2018]:= << Quaternions` ;
 $\beta_0$  = Quaternion[1, 0, 0, 0];
 $\beta_1$  = Quaternion[0, 1, 0, 0];
 $\beta_2$  = Quaternion[0, 0, 1, 0];
 $\beta_3$  = Quaternion[0, 0, 0, 1];
Qcoordinates = { $\beta_1$ ,  $\beta_2$ ,  $\beta_3$ };
m = 400000;
trialDeg = 720;
Ls1 = ConstantArray[0, m];
Ls2 = ConstantArray[0, m];
 $\lambda$  = ConstantArray[0, m];
 $\lambda_2$  = ConstantArray[0, m];
outA = Table[{0, 0, 0, 0, 0}, m];
outB = Table[{0, 0, 0, 0, 0}, m];
outA1 = Table[{0, 0, 0, 0, 0}, m];
outB1 = Table[{0, 0, 0, 0, 0}, m];
outA2 = Table[{0, 0, 0, 0, 0}, m];
outB2 = Table[{0, 0, 0, 0, 0}, m];
listAa1 = Table[{0, 0, 0, 0, 0}, m];
listBb1 = Table[{0, 0, 0, 0, 0}, m];
listAa2 = Table[{0, 0, 0, 0, 0}, m];
listBb2 = Table[{0, 0, 0, 0, 0}, m];
listAa6 = Table[{0, 0, 0, 0, 0}, m];
listBb6 = Table[{0, 0, 0, 0, 0}, m];
listAa7 = Table[{0, 0, 0, 0, 0}, m];
listBb7 = Table[{0, 0, 0, 0, 0}, m];
a1 = ConstantArray[0, m];
b1 = ConstantArray[0, m];
A1 = ConstantArray[0, m];
B1 = ConstantArray[0, m];
nPP = ConstantArray[0, trialDeg];
nNN = ConstantArray[0, trialDeg];
nPN = ConstantArray[0, trialDeg];
nNP = ConstantArray[0, trialDeg];
nAP = ConstantArray[0, trialDeg];
nBP = ConstantArray[0, trialDeg];
nAN = ConstantArray[0, trialDeg];
nBN = ConstantArray[0, trialDeg];
```

Generate Particle Data with 3 Do Loops

```

In[2056]:= Do[e = RandomReal[{-179, 180}]; (*Singlet vector angle*)
  ee = N[Flatten[{FromPolarCoordinates[{1, e *  $\pi$ /180}], 0}]];
   $\lambda$ 2[[i]] = Sign[e]; (*Hidden Variable*)
  Ls1[[i]] =  $\lambda$ 2[[i]] * ee.Qcoordinates;
  Ls2[[i]] = -Ls1[[i]];
   $\lambda$ [[i]] = 0.25 (Cos[ $\frac{e}{2}$ ]^2), {i, m} (*Hidden Variable*)

In[2057]:= Do[a = RandomInteger[{-179, 180}]; (*Detector vector angle 1 degree increments*)
  aa = N[Flatten[{FromPolarCoordinates[{1, a *  $\pi$ /180}], 0}]];
  Da = aa.Qcoordinates; (*Convert to quaternion coordinates*)
  qa = Da ** Ls1[[i]];
  If[Abs[Re[qa]] <  $\lambda$ [[i]], C1 = f1, C1 = g1];
  If[Abs[Re[qa]] >  $\lambda$ [[i]], A = Sign[Re[qa]], A =  $\lambda$ 2[[i]] * Sign[qa[[4]]]];
  AA =  $\lambda$ 2[[i]] * Sign[qa[[4]]];
  outA[[i]] = {a, A, i, C1, AA}, {i, m}

In[2058]:= Do[b = RandomInteger[{-179, 180}]; (*Detector vector angle 1 degree increments*)
  bb = N[Flatten[{FromPolarCoordinates[{1, b *  $\pi$ /180}], 0}]];
  Db = bb.Qcoordinates; (*Convert to quaternion coordinates*)
  qb = Ls2[[i]] ** Db;
  If[Abs[Re[qb]] <  $\lambda$ [[i]], C2 = f2, C2 = g2];
  If[Abs[Re[qb]] >  $\lambda$ [[i]], B = Sign[Re[qb]], B = - $\lambda$ 2[[i]] * Sign[qb[[4]]]];
  BB = - $\lambda$ 2[[i]] * Sign[qb[[4]]];
  outB[[i]] = {b, B, i, C2, BB}, {i, m}

```

## Match Trial Numbers and do Statistical Analysis of Particle Data

```

In[2059]:= outA1 = Select[outA, MemberQ[#, g1] &];
outA2 = Select[outA, MemberQ[#, f1] &];
outB1 = Select[outB, MemberQ[#, g2] &];
outB2 = Select[outB, MemberQ[#, f2] &];
listad = outA1[[All, 3]]; (*Match Trial Numbers*)
listbd = outB1[[All, 3]];
listAa1 = Select[outA1, Intersection[#[[3]], listbd] == {[3]} &];
listBb1 = Select[outB1, Intersection[#[[3]], listad] == {[3]} &];
listad2 = outA1[[All, 3]];
listad3 = listAa1[[All, 3]];
listAa3 = Select[outA1, Intersection[#[[3]], listad3] != {[3]} &];
listAa4 = Select[listAa1, Intersection[#[[3]], listad2] != {[3]} &];
listbd2 = outB1[[All, 3]];
listbd3 = listBb1[[All, 3]];
listBb3 = Select[outB1, Intersection[#[[3]], listbd3] != {[3]} &];
listBb4 = Select[listBb1, Intersection[#[[3]], listbd2] != {[3]} &];
M = Length[listAa3];
listAa7 = Table[{0, 0, 0, 0, 0}, M];
a2 = ConstantArray[0, M];
A2 = ConstantArray[0, M];
ind2 = ConstantArray[0, M];
A3 = ConstantArray[0, M];
A5 = ConstantArray[0, M];
A4 = ConstantArray[0, M];
A6 = ConstantArray[0, M];
a2 = listAa3[[All, 1]];
A2 = listAa3[[All, 2]];

```

```

ind2 = listAa3[All, 3];
A5 = listAa3[All, 5];
Do[A4 = A2[[i]]; A6 = A5[[i]];
  If[A4 == A6, A2 = A2, A2 = A5];
  listAa7[[i]] = {a2[[i]], A2[[i]], ind2[[i]], f1, A5[[i]]}, {i, M}
M2 = Length[listBb3];
listBb7 = Table[{0, 0, 0, 0, 0}, M2];
b2 = ConstantArray[0, M2];
B2 = ConstantArray[0, M2];
ind3 = ConstantArray[0, M2];
B3 = ConstantArray[0, M2];
B5 = ConstantArray[0, M2];
B4 = ConstantArray[0, M2];
B6 = ConstantArray[0, M2];
b2 = listBb3[All, 1];
B2 = listBb3[All, 2];
ind3 = listBb3[All, 3];
B5 = listBb3[All, 5];
Do[B4 = B2[[i]]; B6 = B5[[i]];
  If[B4 == B6, B2 = B2, B2 = B5];
  listBb7[[i]] = {b2[[i]], B2[[i]], ind3[[i]], f1, B5[[i]]}, {i, M2}
outA4 = Sort[Catenate[{outA2, listAa7}], #1[[3]] < #2[[3]] &];
outB4 = Sort[Catenate[{outB2, listBb7}], #1[[3]] < #2[[3]] &];
outA5 = Sort[Catenate[{listAa1, outA4}], #1[[3]] < #2[[3]] &];
outB5 = Sort[Catenate[{listBb1, outB4}], #1[[3]] < #2[[3]] &];
trials2 = Length[outA5];
a1 = outA5[All, 1];
b1 = outB5[All, 1];
A1 = outA5[All, 2];
B1 = outB5[All, 2];
Do[ $\theta$  = a1[[j]] - b1[[j]] + 360; (*All angles are shifted by 2 $\pi$  since  $\theta$  is an index*)
  aliceD = A1[[j]]; bobD = B1[[j]];
  If[aliceD == 1, nAP[[ $\theta$ ]] ++];
  If[bobD == 1, nBP[[ $\theta$ ]] ++];
  If[aliceD == -1, nAN[[ $\theta$ ]] ++];
  If[bobD == -1, nBN[[ $\theta$ ]] ++];
  If[aliceD == 1 && bobD == 1, nPP[[ $\theta$ ]] ++];
  If[aliceD == 1 && bobD == -1, nPN[[ $\theta$ ]] ++];
  If[aliceD == -1 && bobD == 1, nNP[[ $\theta$ ]] ++];
  If[aliceD == -1 && bobD == -1, nNN[[ $\theta$ ]] ++], {j, trials2}

```

## Calculate Mean Values and Plot

```

In[2109]:= pPP = 0; pPN = 0; pNP = 0; pNN = 0;
mean = ConstantArray[0, trialDeg];
Do[sum = nPP[[i]] + nPN[[i]] + nNP[[i]] + nNN[[i]];
  If[sum == 0, Goto[jump],
    {pPP = nPP[[i]] / sum;
    pNP = nNP[[i]] / sum;
    pPN = nPN[[i]] / sum;
    pNN = nNN[[i]] / sum;
  };
  mean[[i]] = pPP + pNN - pPN - pNP];
Label[jump], {i, trialDeg}

```

```

In[2112]:= simulation = ListPlot[mean, PlotMarkers → {Automatic, Tiny}];
negcos = Plot[-Cos[x Degree], {x, 0, 720}, PlotStyle → {Magenta},
  Ticks → {{{0, -360 °}, {90, -270 °}, {180, -180 °}, {270, -90 °}, {360, 0 °}, {450, 90 °},
    {540, 180 °}, {630, 270 °}, {720, 360 °}}, Automatic}, GridLines → Automatic];
p1 = Plot[-1 + 2 x Degree / π, {x, 0, 180}, PlotStyle → {Gray, Dashed}];
p2 = Plot[3 - 2 x Degree / π, {x, 180, 360}, PlotStyle → {Gray, Dashed}];
p3 = Plot[-5 + 2 x Degree / π, {x, 360, 540}, PlotStyle → {Gray, Dashed}];
p4 = Plot[7 - 2 x Degree / π, {x, 540, 720}, PlotStyle → {Gray, Dashed}];

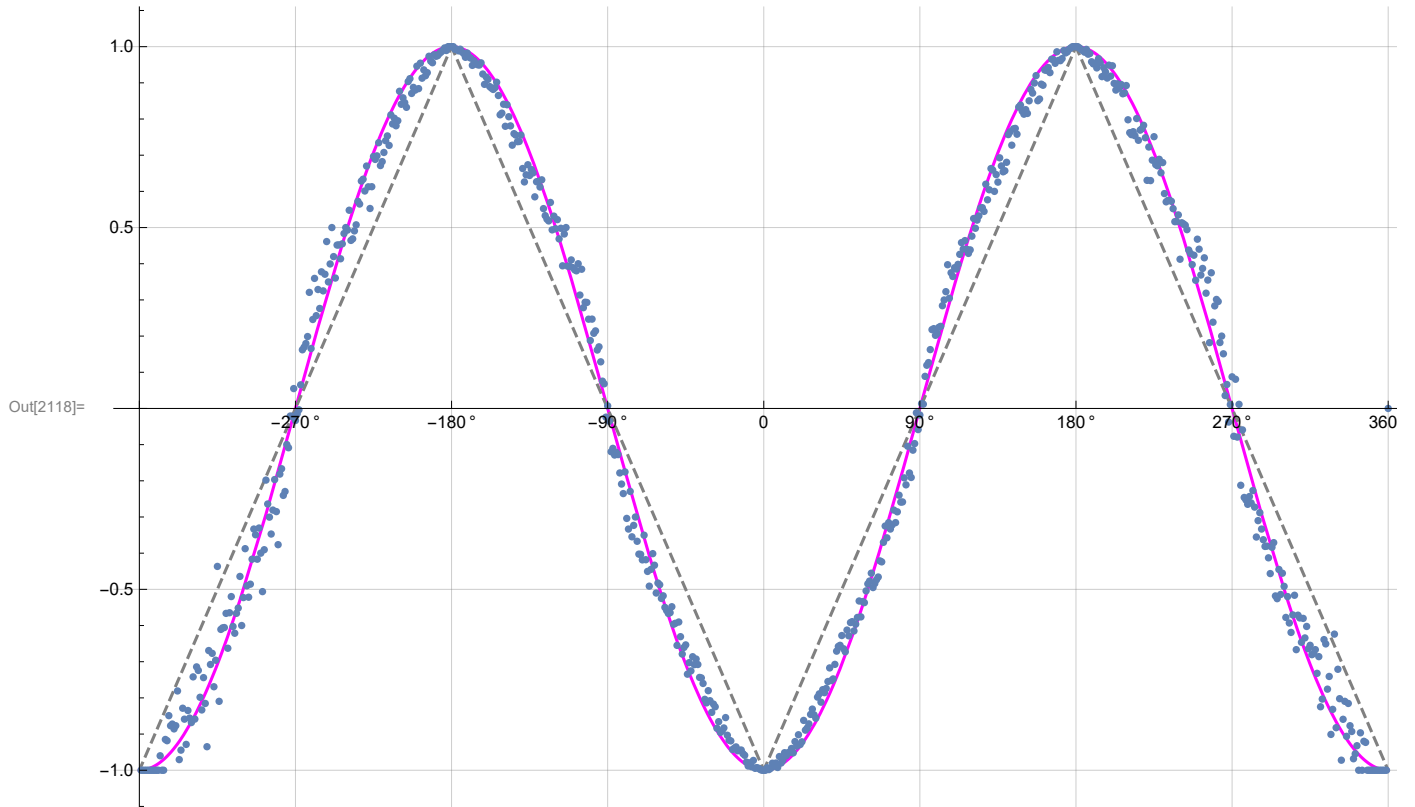
```

Compare mean values with -Cosine Curve and compute averages

```

In[2118]:= Show[negcos, p1, p2, p3, p4, simulation]

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```

In[2119]:= AveA = N[Sum[A1[[i]], {i, trials2}]/trials2];
AveB = N[Sum[B1[[i]], {i, trials2}]/trials2];
Print["AveA = ", AveA]
Print["AveB = ", AveB]
PAP = N[Sum[nAP[[i]], {i, trialDeg}]];
PBP = N[Sum[nBP[[i]], {i, trialDeg}]];
PAN = N[Sum[nAN[[i]], {i, trialDeg}]];
PBN = N[Sum[nBN[[i]], {i, trialDeg}]];
PA1 = PAP / (PAP + PAN);
PB1 = PBP / (PBP + PBN);
Print["P (A+) = ", PA1]
Print["P (B+) = ", PB1]
totAB = Sum[nPP[[i]] + nNN[[i]] + nPN[[i]] + nNP[[i]], {i, trialDeg}]
PP = N[Sum[nPP[[i]], {i, trialDeg}]/totAB]
NN = N[Sum[nNN[[i]], {i, trialDeg}]/totAB]
PN = N[Sum[nPN[[i]], {i, trialDeg}]/totAB]
NP = N[Sum[nNP[[i]], {i, trialDeg}]/totAB]
CHSH = Abs [N[mean[ [315] ] ] - N[mean[ [225] ] ] + N[mean[ [405] ] ] + N[mean[ [45] ] ] ]

AveA = 0.000435
AveB = 0.001635
P (A+) = 0.500218
P (B+) = 0.500818

Out[2131]= 400 000

Out[2132]= 0.250188

Out[2133]= 0.249153

Out[2134]= 0.25003

Out[2135]= 0.25063

Out[2136]= 2.36179

In[2137]:= trials2
Out[2137]= 400 000

```