

**Simulation Based on Michel Fodje's epr-simple simulation translated from
Python to Mathematica by John Reed 13 Nov 2013
Modified by Fred Diether for Completely Local-Realistic Aug 2021
Some matching parts by Bill Nelson**

Set Run Time Parameters, Initialize Arrays and Tables

```
In[*]:= m = 400000;
trialDeg = 721;
s = ConstantArray[0, m];
λ = ConstantArray[0, m];
outA = Table[{0, 0, 0, 0, 0}, m];
outB = Table[{0, 0, 0, 0, 0}, m];
outA4 = Table[{0, 0, 0, 0, 0}, m];
outB4 = Table[{0, 0, 0, 0, 0}, m];
a1 = ConstantArray[0, m];
b1 = ConstantArray[0, m];
A = ConstantArray[0, m];
B = ConstantArray[0, m];
nPP = ConstantArray[0, trialDeg];
nNN = ConstantArray[0, trialDeg];
nPN = ConstantArray[0, trialDeg];
nNP = ConstantArray[0, trialDeg];
nAP = ConstantArray[0, trialDeg];
nBP = ConstantArray[0, trialDeg];
nAN = ConstantArray[0, trialDeg];
nBN = ConstantArray[0, trialDeg];
η = 3;
β = 0.3;
ξ = -15;
```

Generate Particle Data with 3 Do Loops

```
In[*]:= Do[e = RandomReal[{0, 360}]; (*Singlet vector angle*)
s[[i]] = e;
λ[[i]] = β Cos[ $\frac{e}{\eta}$ ]^2, (*Hidden Variables*)
{i, m}]

In[*]:= Do[a = RandomInteger[{0, 360}]; (*Detector vector angle 1 degree increments*)
If[Abs[Cos[(a - s[[i]]) Degree]] < λ[[i]], C1 = f1, C1 = g1];
If[Abs[Cos[(a - s[[i]]) Degree]] > λ[[i]],
Aa = -Sign[Cos[(a - s[[i]]) Degree]], Aa = -Sign[Sin[(a - s[[i]] + ξ) Degree]]];
A5 = -Sign[Sin[(a - s[[i]] + ξ) Degree]];
outA4[[i]] = {a, Aa, i, C1, A5}, {i, m}
outA1 = Select[outA4, MemberQ[#, g1] &];
outA2 = Select[outA4, MemberQ[#, f1] &];
```

```

In[*]:= Do[b = RandomInteger[{0, 360}]; (*Detector vector angle 1 degree increments*)
  If[Abs[Cos[(b - s[[i]]) Degree]] < λ[[i]], C2 = f2, C2 = g2];
  If[Abs[Cos[(b - s[[i]]) Degree]] > λ[[i]],
    Bb = Sign[Cos[(b - s[[i]]) Degree]], Bb = Sign[Sin[(b - s[[i]] + ξ) Degree]]];
  B5 = Sign[Sin[(b - s[[i]] + ξ) Degree]];
  outB4[[i]] = {b, Bb, i, C2, B5}, {i, m}
outB1 = Select[outB4, MemberQ[#, g2] &];
outB2 = Select[outB4, MemberQ[#, f2] &];

```

Match Events Using Trial Numbers

```

In[*]:= listad = outA1[[All, 3]];
listbd = outB1[[All, 3]];

```

Local Detection Analysis of Events Observed by Alice

```

In[*]:= listA4 = Select[outA1, Intersection[{#[[3]]}, listbd] == {#[[3]]} &];
listad2 = outA1[[All, 3]];
listad3 = listA4[[All, 3]];
listA3 = Select[outA1, Intersection[{#[[3]]}, listad3] != {#[[3]]} &];
listAa4 = Select[listA4, Intersection[{#[[3]]}, listad2] != {#[[3]]} &];
M = Length[listA3];
listA6 = Table[{0, 0, 0, 0, 0}, M];
a2 = ConstantArray[0, M];
A2 = ConstantArray[0, M];
ind2 = ConstantArray[0, M];
A3 = ConstantArray[0, M];
A7 = ConstantArray[0, M];
A4 = ConstantArray[0, M];
A6 = ConstantArray[0, M];
a2 = listA3[[All, 1]];
A2 = listA3[[All, 2]];
ind2 = listA3[[All, 3]];
A7 = listA3[[All, 5]];
Do[A4 = A2[[i]]; A6 = A7[[i]];
  If[A4 == A6, A2 = A2, A7 = A7];
  listA6[[i]] = {a2[[i]], A2[[i]], ind2[[i]], f1, A7[[i]]}, {i, M}
outA = Sort[Catenate[{listA4, outA2, listA6}], #1[[3]] < #2[[3]] &];
a1 = outA[[All, 1]];
A = outA[[All, 2]];

```

Local Detection Analysis of Events Observed by Bob

```

In[*]:= listB4 = Select[outB1, Intersection[{#[[3]]}, listad] == {#[[3]]} &];
listbd2 = outB1[[All, 3]];
listbd3 = listB4[[All, 3]];
listB3 = Select[outB1, Intersection[{#[[3]]}, listbd3] != {#[[3]]} &];
listBb4 = Select[listB4, Intersection[{#[[3]]}, listbd2] != {#[[3]]} &];
M2 = Length[listB3];
listB6 = Table[{0, 0, 0, 0, 0}, M2];
b2 = ConstantArray[0, M2];
B2 = ConstantArray[0, M2];
ind3 = ConstantArray[0, M2];
B3 = ConstantArray[0, M2];
B7 = ConstantArray[0, M2];
B4 = ConstantArray[0, M2];
B6 = ConstantArray[0, M2];
b2 = listB3[[All, 1]];
B2 = listB3[[All, 2]];
ind3 = listB3[[All, 3]];
B7 = listB3[[All, 5]];
Do[B4 = B2[[i]]; B6 = B7[[i]];
  If[B4 == B6, B2 = B2, B2 = B7];
  listB6[[i]] = {b2[[i]], B2[[i]], ind3[[i]], f1, B7[[i]]}, {i, M2}];
outB = Sort[Catenate[{listB4, outB2, listB6}], #1[[3]] < #2[[3]] &];
b1 = outB[[All, 1]];
B = outB[[All, 2]];

```

Statistical Analysis of Particle Data

```

In[*]:= Do[ $\theta$  = a1[[j]] - b1[[j]] + 361; (*All angles are shifted by  $2\pi$  since  $\theta$  is an index*)
  aliceD = A[[j]]; bobD = B[[j]];
  If[aliceD == 1, nAP[[ $\theta$ ]] ++];
  If[bobD == 1, nBP[[ $\theta$ ]] ++];
  If[aliceD == -1, nAN[[ $\theta$ ]] ++];
  If[bobD == -1, nBN[[ $\theta$ ]] ++];
  If[aliceD == 1 && bobD == 1, nPP[[ $\theta$ ]] ++];
  If[aliceD == 1 && bobD == -1, nPN[[ $\theta$ ]] ++];
  If[aliceD == -1 && bobD == 1, nNP[[ $\theta$ ]] ++];
  If[aliceD == -1 && bobD == -1, nNN[[ $\theta$ ]] ++], {j, m}];

```

Calculate Mean Values and Plot

```

In[*]:= pPP = 0; pPN = 0; pNP = 0; pNN = 0;
mean = ConstantArray[0, trialDeg];
Do[sum = nPP[[i]] + nPN[[i]] + nNP[[i]] + nNN[[i]];
  If[sum == 0, Goto[jump],
    {pPP = nPP[[i]] / sum;
     pNP = nNP[[i]] / sum;
     pPN = nPN[[i]] / sum;
     pNN = nNN[[i]] / sum;
    mean[[i]] = pPP + pNN - pPN - pNP}];
  Label[jump], {i, trialDeg}];

```

```

In[ ]:= simulation = ListPlot[mean, PlotMarkers → {Automatic, Tiny}];
negcos = Plot[-Cos[x Degree], {x, 0, 720}, PlotStyle → {Magenta},
  Ticks → {{0, -360 °}, {90, -270 °}, {180, -180 °}, {270, -90 °}, {360, 0 °}, {450, 90 °},
    {540, 180 °}, {630, 270 °}, {720, 360 °}}, Automatic, GridLines → Automatic];
p1 = Plot[-1 + (2 x Degree) / π, {x, 0, 180}, PlotStyle → {Gray, Dashed}];
p2 = Plot[3 - 2 x Degree / π, {x, 180, 360}, PlotStyle → {Gray, Dashed}];
p3 = Plot[-5 + 2 x Degree / π, {x, 360, 540}, PlotStyle → {Gray, Dashed}];
p4 = Plot[7 - 2 x Degree / π, {x, 540, 720}, PlotStyle → {Gray, Dashed}];

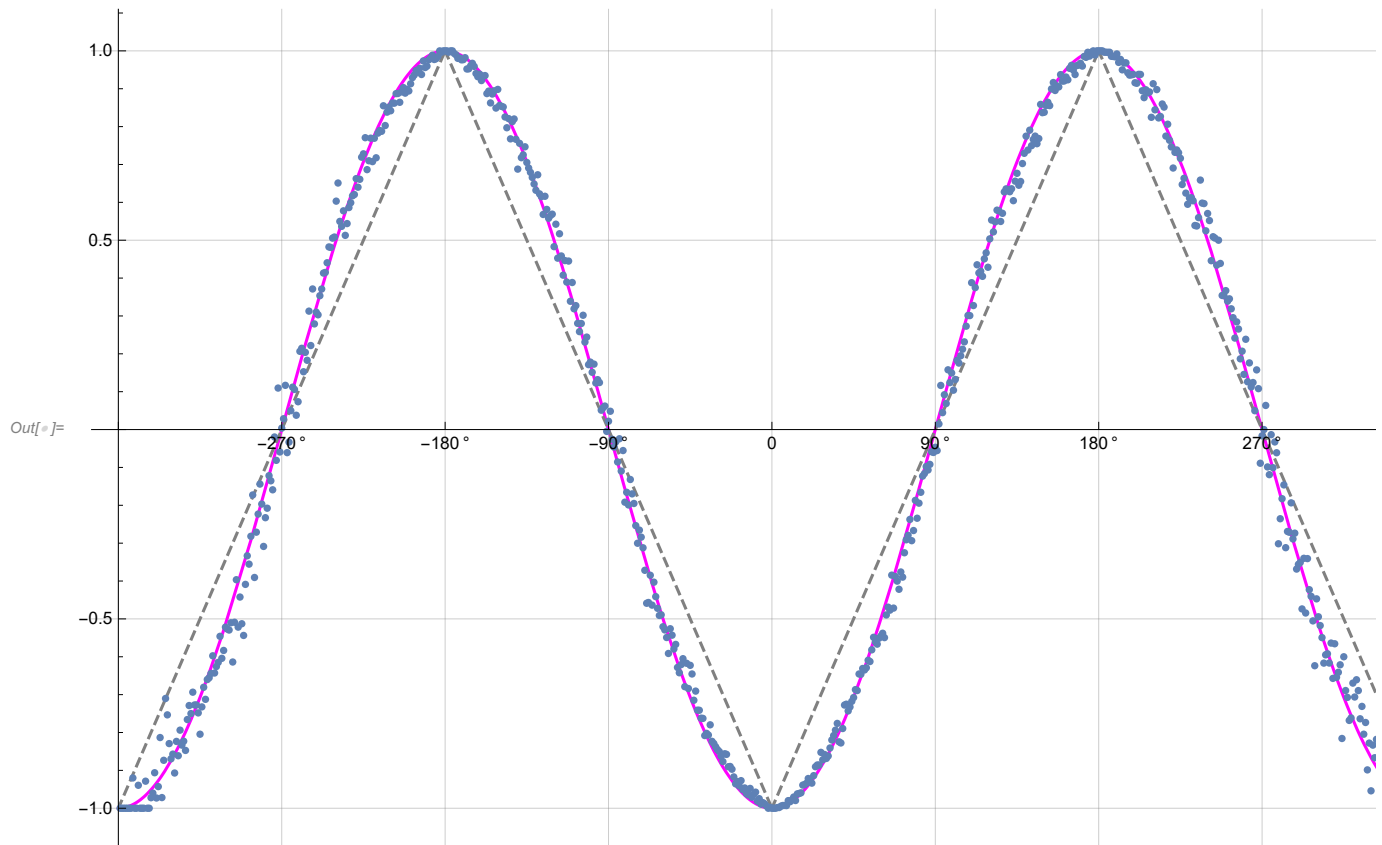
```

Compare mean values with -Cosine Curve and compute averages

```

In[ ]:= Show[negcos, p1, p2, p3, p4, simulation]

```



```

In[ ]:= AveA = N[Sum[A[[i]], {i, m}]/m];
AveB = N[Sum[B[[i]], {i, m}]/m];
Print["AveA = ", AveA]
Print["AveB = ", AveB]
PAP = N[Sum[nAP[[i]], {i, trialDeg}]];
PBP = N[Sum[nBP[[i]], {i, trialDeg}]];
PAN = N[Sum[nAN[[i]], {i, trialDeg}]];
PBN = N[Sum[nBN[[i]], {i, trialDeg}]];
PA1 = PAP / (PAP + PAN);
PB1 = PBP / (PBP + PBN);
Print["P(A+) = ", PA1]
Print["P(B+) = ", PB1]
totAB = Sum[nPP[[i]] + nNN[[i]] + nPN[[i]] + nNP[[i]], {i, trialDeg}]
PP = N[Sum[nPP[[i]], {i, trialDeg}]/totAB]
NN = N[Sum[nNN[[i]], {i, trialDeg}]/totAB]
PN = N[Sum[nPN[[i]], {i, trialDeg}]/totAB]
NP = N[Sum[nNP[[i]], {i, trialDeg}]/totAB]
CHSH = Abs[N[mean[[315]]] - N[mean[[225]]] + N[mean[[405]]] + N[mean[[45]]]]

AveA = -0.001525

AveB = 0.00118

P(A+) = 0.499238

P(B+) = 0.50059

Out[ ]:= 400 000

Out[ ]:= 0.2495

Out[ ]:= 0.249673

Out[ ]:= 0.249738

Out[ ]:= 0.25109

Out[ ]:= 2.8401

```