

**Simulation Based on Michel Fodje's epr-simple simulation translated from
Python to Mathematica by John Reed 13 Nov 2013
Modified by Fred Diether for Completely Local-Realistic Sep 2021
Some parts by Bill Nelson.**

Set Run Time Parameters, Initialize Arrays and Tables

```
In[2106]:= m = 5000000;
trialDeg = 721;
s1 = ConstantArray[0, m];
s2 = ConstantArray[0, m];
λ1 = ConstantArray[0, m];
λ2 = ConstantArray[0, m];
outA1 = Table[{0, 0}, m];
outA2 = Table[{0, 0}, m];
outB1 = Table[{0, 0}, m];
outB2 = Table[{0, 0}, m];
aa = ConstantArray[0, m];
bb = ConstantArray[0, m];
a1 = ConstantArray[0, m];
b1 = ConstantArray[0, m];
A = ConstantArray[0, m];
B = ConstantArray[0, m];
nPP = ConstantArray[0, trialDeg];
nNN = ConstantArray[0, trialDeg];
nPN = ConstantArray[0, trialDeg];
nNP = ConstantArray[0, trialDeg];
nAP = ConstantArray[0, trialDeg];
nBP = ConstantArray[0, trialDeg];
nAN = ConstantArray[0, trialDeg];
nBN = ConstantArray[0, trialDeg];
φ = 3; β = 0.32; ξ = 0; (*Adjustable parameters for fine tuning*)
```

Generating Particle Data with Three Independent Do-Loops

```
In[2131]:= Do[θ = RandomReal[{0, 360}]; (*Singlet vector angle*) (*Hidden Variable*)
λ1[[i]] = β (Cos[ $\frac{\theta}{\phi}$ ]^2);
λ2[[i]] = 0.938 (Cos[ $\frac{\theta}{\phi}$ ]^2);
s1[[i]] = θ;
s2[[i]] = θ + 180, {i, m}] (*Conservation of angular momentum*)

In[2132]:= Do[a = RandomInteger[{0, 360}]; (*Detector vector angle 1 degree increments*)
aa[[i]] = a;
If[Abs[Cos[(a - s1[[i])] Degree]] > λ1[[i]], Aa1 = Sign[Cos[(a - s1[[i])] Degree]], Aa1 = 0];
outA1[[i]] = {a, Aa1}, {i, m}]
Do[If[Abs[Cos[(aa[[i]] - s1[[i])] Degree]] < λ2[[i]],
Aa2 = Sign[Sin[(aa[[i]] - s1[[i]] + ξ) Degree]], Aa2 = 0];
outA2[[i]] = {aa[[i]], Aa2}, {i, m}]
outA = Catenate[{outA1, outA2}];
a1 = outA[[All, 1]];
A = outA[[All, 2]];
```

```

In[2137]:= Do[b = RandomInteger[{0, 360}]; (*Detector vector angle 1 degree increments*)
  bb[[i]] = b;
  If[Abs[Cos[(b - s2[[i]]) Degree]] > λ1[[i]], Bb1 = Sign[Cos[(b - s2[[i]]) Degree]], Bb1 = 0];
  outB1[[i]] = {b, Bb1}, {i, m}
Do[If[Abs[Cos[(bb[[i]] - s2[[i]]) Degree]] < λ2[[i]],
  Bb2 = Sign[Sin[(bb[[i]] - s2[[i]] + ξ) Degree]], Bb2 = 0];
  outB2[[i]] = {bb[[i]], Bb2}, {i, m}
outB = Catenate[{outB1, outB2}];
b1 = outB[[All, 1]];
B = outB[[All, 2]];

```

Statistical Analysis of the Particle Data Received from Alice and Bob

```

In[2142]:= m2 = 2 m;
Do[θ1 = a1[[j]] - b1[[j]] + 361;
  (*All angles are shifted by 361 degrees since θ1 is an index*)
  aliceD = A[[j]]; bobD = B[[j]];
  If[aliceD == 1, nAP[[θ1]] ++];
  If[bobD == 1, nBP[[θ1]] ++];
  If[aliceD == -1, nAN[[θ1]] ++];
  If[bobD == -1, nBN[[θ1]] ++];
  If[aliceD == 1 && bobD == 1, nPP[[θ1]] ++];
  If[aliceD == 1 && bobD == -1, nPN[[θ1]] ++];
  If[aliceD == -1 && bobD == 1, nNP[[θ1]] ++];
  If[aliceD == -1 && bobD == -1, nNN[[θ1]] ++], {j, m2}

```

Calculating Mean Values of A, B, and AB, and Plotting the Results

```

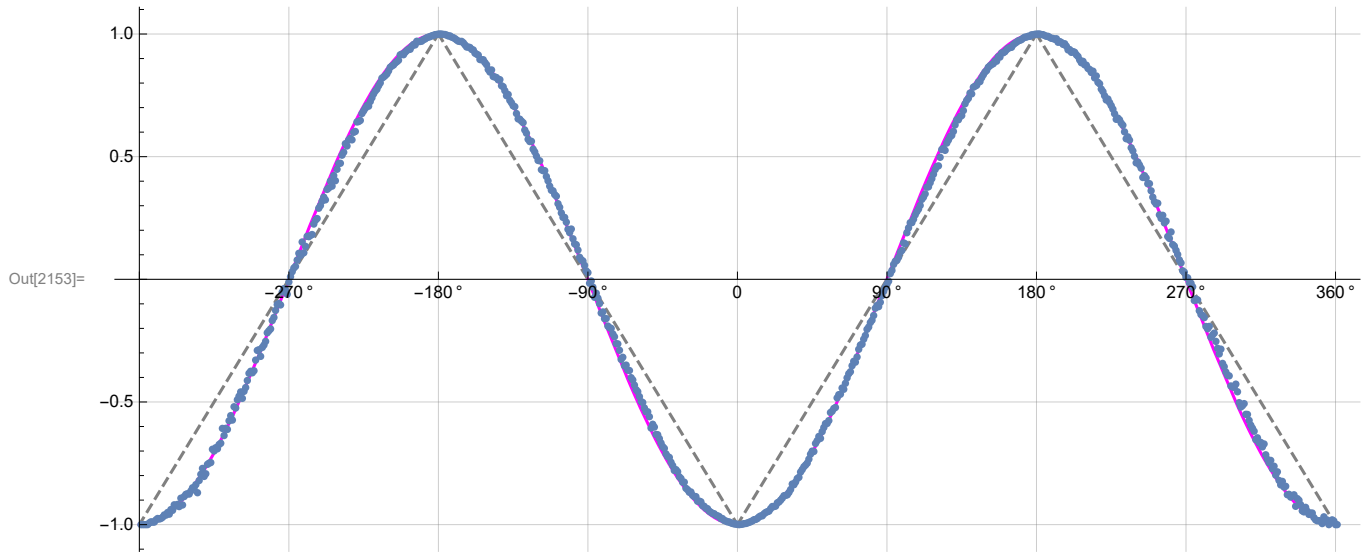
In[2144]:= pPP = 0; pPN = 0; pNP = 0; pNN = 0;
mean = ConstantArray[0, trialDeg];
Do[sum = nPP[[i]] + nPN[[i]] + nNP[[i]] + nNN[[i]];
  If[sum == 0, Goto[jump],
    {pPP = nPP[[i]] / sum;
     pNP = nNP[[i]] / sum;
     pPN = nPN[[i]] / sum;
     pNN = nNN[[i]] / sum;
    mean[[i]] = pPP + pNN - pPN - pNP}];
  Label[jump], {i, trialDeg}

In[2147]:= simulation = ListPlot[mean, PlotMarkers → {Automatic, Tiny}];
negcos = Plot[-Cos[x Degree], {x, 0, 720}, PlotStyle → {Magenta}, AspectRatio → 7 / 16,
  Ticks → {{0, -360 °}, {90, -270 °}, {180, -180 °}, {270, -90 °}, {360, 0 °}, {450, 90 °},
    {540, 180 °}, {630, 270 °}, {720, 360 °}}, Automatic, GridLines → Automatic];
p1 = Plot[-1 + 2 x Degree / π, {x, 0, 180}, PlotStyle → {Gray, Dashed}];
p2 = Plot[3 - 2 x Degree / π, {x, 180, 360}, PlotStyle → {Gray, Dashed}];
p3 = Plot[-5 + 2 x Degree / π, {x, 360, 540}, PlotStyle → {Gray, Dashed}];
p4 = Plot[7 - 2 x Degree / π, {x, 540, 720}, PlotStyle → {Gray, Dashed}];

```

Comparing Mean Values with -Cosine Function and Computing Averages

In[2153]:= Show[negcos, p1, p2, p3, p4, simulation]



```
In[2154]:= AveA = N[Sum[A[[i]], {i, m}]/m];
AveB = N[Sum[B[[i]], {i, m}]/m];
Print["AveA = ", AveA]
Print["AveB = ", AveB]
PAP = N[Sum[nAP[[i]], {i, trialDeg}]];
PBP = N[Sum[nBP[[i]], {i, trialDeg}]];
PAN = N[Sum[nAN[[i]], {i, trialDeg}]];
PBN = N[Sum[nBN[[i]], {i, trialDeg}]];
PA1 = PAP / (PAP + PAN);
PB1 = PBP / (PBP + PBN);
Print["P(A+) = ", PA1]
Print["P(B+) = ", PB1]
totAB = Sum[nPP[[i]] + nNN[[i]] + nPN[[i]] + nNP[[i]], {i, trialDeg}];
Print["Total Events = ", totAB]
PP = N[Sum[nPP[[i]], {i, trialDeg}]/totAB];
NN = N[Sum[nNN[[i]], {i, trialDeg}]/totAB];
PN = N[Sum[nPN[[i]], {i, trialDeg}]/totAB];
NP = N[Sum[nNP[[i]], {i, trialDeg}]/totAB];
Print["Ave ++ = ", PP]
Print["Ave -- = ", NN]
Print["Ave +- = ", PN]
Print["Ave -+ = ", NP]
CHSH = Abs[N[mean[[315]]] - N[mean[[225]]] + N[mean[[405]]] + N[mean[[45]]]];
Print["Approx. CHSH = ", CHSH]
```

```

AveA = 0.0003344
AveB = -0.0003312
P(A+) = 0.500103
P(B+) = 0.499816
Total Events = 4991174
Ave ++ = 0.250137
Ave -- = 0.249953
Ave +- = 0.250086
Ave -+ = 0.249824
Approx. CHSH = 2.78929

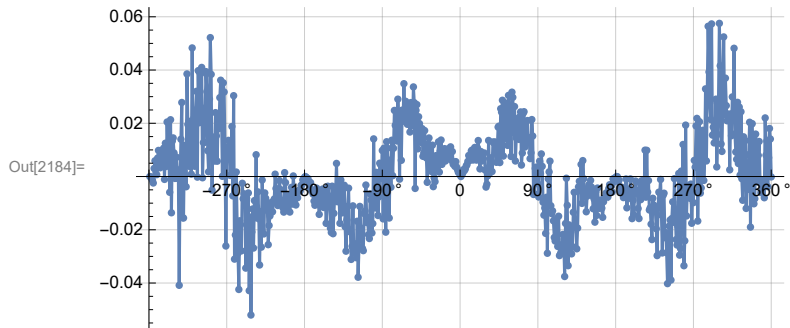
```

Deviation from negative cosine curve

```

In[2178]:= dev1 = ConstantArray[2, 720];
dev2 = ConstantArray[2, 720];
dev3 = ConstantArray[2, 720];
Do[dev1 = mean[[i]]; dev2[[i]] = {dev1, i}, {i, 720}]
devang = dev2[[All, 2]] - 361;
Do[dev3[[i]] = mean[[i]] + Cos[devang[[i]] Degree], {i, 720}]
ListPlot[N[dev3], PlotMarkers -> {Automatic, Tiny}, Joined -> True, AspectRatio -> 1/2,
  Ticks -> {{0, -360 °}, {90, -270 °}, {180, -180 °}, {270, -90 °}, {360, 0 °}, {450, 90 °},
    {540, 180 °}, {630, 270 °}, {720, 360 °}}, Automatic], GridLines -> Automatic]

```



```

In[2185]:= Mean[N[dev3]]
Mean[N[Abs[dev3]]]

```

Out[2185]= 0.000579506

Out[2186]= 0.012917