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trials = 4000;
n1 = ConstantArray[0, trials]; (*container for n1*)
Do[q = RandomPoint[Sphere[4]]; (*uniform random points of a 4 dimensional sphere*)
  w = q[[1]]; (*extracts the first coordinate of q*)
  x = q[[2]]; (*etc.*)
  y = q[[3]];
  z = q[[4]];
  n = {0, 2 w * y + 2 x * z, 2 y * z - 2 w * x, w^2 + z^2 - x^2 - y^2}; (*Niles Johnson's coordinate translation from quaternion math*)
  n1[[j]] = {n[[2]], n[[3]], n[[4]]}, (*extracts the x, y and z coordinates from n; the first coordinate is zero*)
  {j, trials}} (*run the loop for that many trials*)
Graphics3D[Table[Point[{{0, 0, 0}, p}], {p, n1}]] (*plots n1 in 3D*)

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Out[7]=

