

**Michel Fodje's epr-simple simulation translated from
Python to Mathematica by John Reed 13 Nov 2013
Modified for QM Local Complete States 26 Jul 2019 2D Vectors**

Set run time parameters, initialize arrays

```
In[828]:= trials = 5 000 000;  
trialDeg = 360;
```

```
In[830]:= aliceDeg = ConstantArray[0, trials];  
bobDeg = ConstantArray[0, trials];  
aliceDet = ConstantArray[0, trials];  
bobDet = ConstantArray[0, trials];  
a1 = ConstantArray[0, trials];  
b1 = ConstantArray[0, trials];
```

```
In[836]:= nPP = ConstantArray[0, trialDeg];  
nNN = ConstantArray[0, trialDeg];  
nPN = ConstantArray[0, trialDeg];  
nNP = ConstantArray[0, trialDeg];  
nAP = ConstantArray[0, trialDeg];  
nBP = ConstantArray[0, trialDeg];  
nAN = ConstantArray[0, trialDeg];  
nBN = ConstantArray[0, trialDeg];
```

Generate Particle Data

```

In[844]:= Do[
  z = (1/2) Sin[RandomReal[{0, π/2}]]^2; (*Complete States Parameter*)
  λ = RandomChoice[{-1, 1}];
  s = Flatten[List[Normalize@RandomVariate[NormalDistribution[], 2], 0], 1];
  a = Flatten[List[Normalize@RandomVariate[NormalDistribution[], 2], 0], 1];
  x1 = Part[a, 1]; y1 = Part[a, 2];
  aliceDeg[[i]] = ArcTan[x1, x2];
  a1[[i]] = a;
  b = Flatten[List[Normalize@RandomVariate[NormalDistribution[], 2], 0], 1];
  x2 = Part[b, 1]; y2 = Part[b, 2];
  bobDeg[[i]] = ArcTan[x2, y2];
  b1[[i]] = b;
  If[a.s > 0, s1 = a, s1 = -a]; (*Polarizer Functions*)
  If[b.s > 0, s2 = b, s2 = -b];
  (*Measurement Functions*)
  If[Abs[a.s] < z, A = {0 + 0. i},
    A = 
$$\frac{\lambda}{2} \left( \begin{pmatrix} 1 & 0 \end{pmatrix} \cdot (\text{PauliMatrix}[1] * a[[1]] + \text{PauliMatrix}[2] * a[[2]] + \text{PauliMatrix}[3] * a[[3]]) \cdot \right.$$


$$\left. (\text{PauliMatrix}[1] * (-s1[[1]]) + \text{PauliMatrix}[2] * (-s1[[2]]) + \right.$$


$$\left. \text{PauliMatrix}[3] * (-s1[[3]]) \right) \cdot \begin{pmatrix} 1 \\ 0 \end{pmatrix} +$$


$$\begin{pmatrix} 0 & 1 \end{pmatrix} \cdot (\text{PauliMatrix}[1] * a[[1]] + \text{PauliMatrix}[2] * a[[2]] + \text{PauliMatrix}[3] * a[[3]]) \cdot$$


$$\left. (\text{PauliMatrix}[1] * (-s1[[1]]) + \text{PauliMatrix}[2] * (-s1[[2]]) + \right.$$


$$\left. \text{PauliMatrix}[3] * (-s1[[3]]) \right) \cdot \begin{pmatrix} 0 \\ 1 \end{pmatrix} \right];$$

    aliceDet[[i]] = Extract[Flatten[Re[A]], 1];
    If[Abs[b.s] < z, B = {0 + 0. i},
      B = 
$$\frac{\lambda}{2} \left( \begin{pmatrix} 1 & 0 \end{pmatrix} \cdot (\text{PauliMatrix}[1] * s2[[1]] + \text{PauliMatrix}[2] * s2[[2]] + \text{PauliMatrix}[3] * s2[[3]]) \cdot \right.$$


$$\left. (\text{PauliMatrix}[1] * b[[1]] + \text{PauliMatrix}[2] * b[[2]] + \text{PauliMatrix}[3] * b[[3]]) \right) \cdot \begin{pmatrix} 1 \\ 0 \end{pmatrix} +$$


$$\begin{pmatrix} 0 & 1 \end{pmatrix} \cdot (\text{PauliMatrix}[1] * s2[[1]] + \text{PauliMatrix}[2] * s2[[2]] + \text{PauliMatrix}[3] * s2[[3]]) \cdot$$


$$\left. (\text{PauliMatrix}[1] * b[[1]] + \text{PauliMatrix}[2] * b[[2]] + \text{PauliMatrix}[3] * b[[3]]) \right) \cdot \begin{pmatrix} 0 \\ 1 \end{pmatrix} \right];$$

      bobDet[[i]] = Extract[Flatten[Re[B]], 1],
    {i, trials}]

```

Statistical Analysis of Particle Data

```

In[845]:= Do[
  If[(aliceDeg[[i]] * bobDeg[[i]]) > 0, theta = ArcCos[a1[[i]].b1[[i]]] * 180/π,
    theta = -ArcCos[a1[[i]].b1[[i]]] * 180/π + 360];
  θ = Round[theta];
  aliceD = aliceDet[[i]]; bobD = bobDet[[i]];
  If[aliceD == 1, nAP[θ]++];
  If[bobD == 1, nBP[θ]++];
  If[aliceD == -1, nAN[θ]++];
  If[bobD == -1, nBN[θ]++];
  If[aliceD == 1 && bobD == 1, nPP[θ]++];
  If[aliceD == 1 && bobD == -1, nPN[θ]++];
  If[aliceD == -1 && bobD == 1, nNP[θ]++];
  If[aliceD == -1 && bobD == -1, nNN[θ]++],
  {i, trials}]

```

Calculate mean values and plot

```

In[846]:= pPP = 0; pPN = 0; pNP = 0; pNN = 0;

In[847]:= mean = ConstantArray[0, trialDeg];

In[848]:= Do[
  sum = nPP[[i]] + nPN[[i]] + nNP[[i]] + nNN[[i]];
  If[sum == 0, Goto[jump],
    {pPP = nPP[[i]] / sum;
     pNP = nNP[[i]] / sum;
     pPN = nPN[[i]] / sum;
     pNN = nNN[[i]] / sum;
    mean[[i]] = pPP + pNN - pPN - pNP}];
  Label[jump],
  {i, trialDeg}]

In[849]:= simulation = ListPlot[mean, PlotMarkers -> {Automatic, Tiny}];

In[850]:= negcos = Plot[-Cos[x Degree], {x, 1, 361}, PlotStyle -> {Red}];

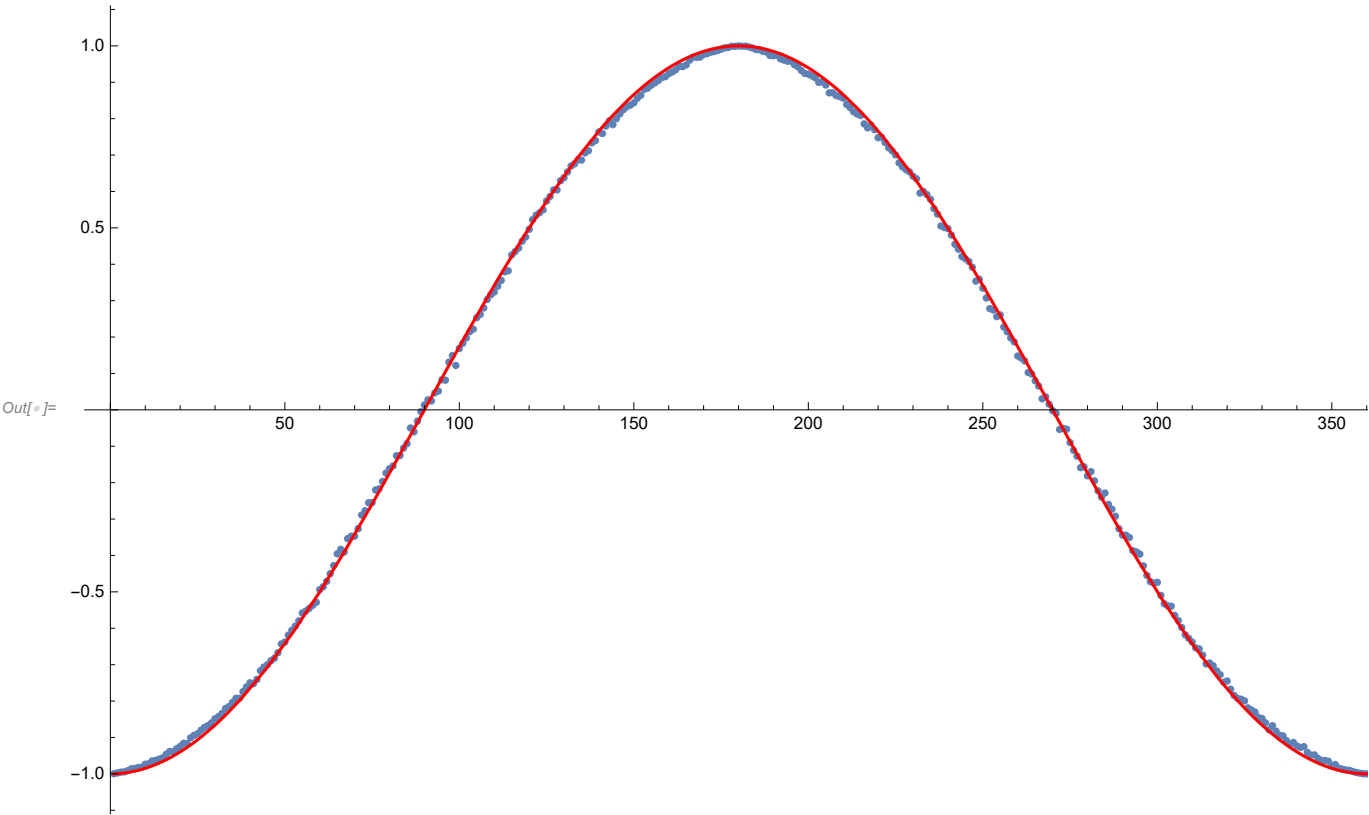
```

Compare mean values with -Cosine Curve and compute averages

```

Show[simulation, negcos]
AveA = N[Sum[aliceDet[[i]], {i, trials}] / trials];
AveB = N[Sum[bobDet[[i]], {i, trials}] / trials];
Print["AveA = ", AveA]
Print["AveB = ", AveB]
PAP = N[Sum[nAP[[i]], {i, trialDeg}]];
PBP = N[Sum[nBP[[i]], {i, trialDeg}]];
PAN = N[Sum[nAN[[i]], {i, trialDeg}]];
PBN = N[Sum[nBN[[i]], {i, trialDeg}]];
PA1 = PAP / (PAP + PAN);
PB1 = PBP / (PBP + PBN);
Print["P(A+) = ", PA1]
Print["P(B+) = ", PB1]
totAB = Sum[nPP[[i]] + nNN[[i]] + nPN[[i]] + nNP[[i]], {i, trialDeg}];
PP = N[Sum[nPP[[i]], {i, trialDeg}] / totAB]
NN = N[Sum[nNN[[i]], {i, trialDeg}] / totAB]
PN = N[Sum[nPN[[i]], {i, trialDeg}] / totAB]
NP = N[Sum[nNP[[i]], {i, trialDeg}] / totAB]

```



AveA = -0.0006222

AveB = -0.0007768

P (A+) = 0.499624

P (B+) = 0.499538

Out[]= 0.249707

Out[]= 0.250575

Out[]= 0.249629

Out[]= 0.249595